

$$\lim_{x \rightarrow \infty} \frac{3x+5}{6x-2}$$

$$\frac{3x}{6x} = \frac{1}{2}$$

$$\lim_{x \rightarrow -\infty} = \frac{1}{2}$$

$$\lim_{x \rightarrow \infty} \frac{3x+5}{6x-2}$$

"8/8" ish
just like
0/0, 8/8 = 1DK

$$= \lim_{x \rightarrow \infty} \frac{x(3 + \frac{5}{x})}{x(6 - \frac{2}{x})}$$

$$= \lim_{x \rightarrow \infty} \frac{3 + \frac{5}{x}}{6 - \frac{2}{x}} = \frac{3+0}{6-0} = \frac{3}{6} = \frac{1}{2}$$

$$\lim_{x \rightarrow -\infty} \frac{4x^2 - x}{2x^3 - 5} \stackrel{"/-"}{=} \lim_{x \rightarrow -\infty} \frac{x^2(4 - \frac{1}{x})}{x^3(2 - \frac{5}{x^3})}$$

$$= \lim_{x \rightarrow -\infty} \frac{4 - \frac{1}{x}}{x(2 - \frac{5}{x^3})}$$

$$\lim_{x \rightarrow -\infty} \frac{4}{x(2)} \quad \swarrow$$

$$= \frac{4 + 0}{\overset{-\infty}{\uparrow} (2 - 0)} = 0$$

$$= \lim_{x \rightarrow -\infty} \left(\frac{2}{x} \right)$$

$$\lim_{x \rightarrow -\infty} \frac{4x^2 - x}{2x^3 - 5} = \lim_{x \rightarrow -\infty} \frac{x(4x - 1)}{x(2x^2 - \frac{5}{x})}$$

$$= \lim_{x \rightarrow -\infty} \frac{4x - 1}{2x^2 - \frac{5}{x}} = \lim_{x \rightarrow -\infty} \frac{x(4 - \frac{1}{x})}{x(2x - \frac{5}{x^2})}$$

$$\frac{4x^2}{2x^3} = \frac{2}{x}$$

$$= \lim_{x \rightarrow -\infty} \frac{4 - \frac{1}{x} \rightarrow 4}{2x - \frac{5}{x^2} \rightarrow -\infty} = 0$$

$$\begin{aligned}
 \lim_{x \rightarrow \infty} \sqrt{\frac{3x+5}{6x-8}} &= \frac{\sqrt{1}}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} \\
 &= \sqrt{\lim_{x \rightarrow \infty} \frac{3x+5}{6x-8}} = \sqrt{\frac{1}{2}} \\
 &= \frac{\sqrt{2}}{2}
 \end{aligned}$$

$$\lim_{x \rightarrow \infty} \frac{\sqrt{x^2+2}}{3x-6} = \lim_{x \rightarrow \infty} \frac{\sqrt{x^2} \sqrt{1+\frac{2}{x^2}}}{x(3-\frac{6}{x})}$$

$$= \lim_{x \rightarrow \infty} \frac{x \sqrt{1+\frac{2}{x^2}}}{x(3-\frac{6}{x})}$$

lim

$$= \lim_{x \rightarrow \infty} \frac{\sqrt{1+\frac{2}{x^2}}}{3-\frac{6}{x}} = \frac{\sqrt{1}}{3} = \frac{1}{3}$$

$$\lim_{x \rightarrow -\infty} \frac{\sqrt{x^2+2}}{3x-6} = \lim_{x \rightarrow -\infty} \frac{\sqrt{x^2} \sqrt{1+\frac{2}{x^2}}}{x(3-\frac{6}{x})}$$

$$= \lim_{x \rightarrow -\infty} \frac{|x| \sqrt{1+\frac{2}{x^2}}}{x(3-\frac{6}{x})}$$

$$= \lim_{x \rightarrow -\infty} \frac{(-x) \sqrt{1+\frac{2}{x^2}}}{x(3-\frac{6}{x})}$$

$$= \lim_{x \rightarrow -\infty} \frac{-\sqrt{1+\frac{2}{x^2}}}{3-\frac{6}{x}}$$

$$= \left(\frac{-1}{3} \right)$$

$$\begin{aligned}
 & \lim_{x \rightarrow \infty} \frac{\sqrt{x^6+5} - x^3}{1} \quad \parallel (a+b)^2 \neq a^2+b^2 \\
 &= \lim_{x \rightarrow \infty} \frac{(\sqrt{x^6+5} - x^3)(\sqrt{x^6+5} + x^3)}{\sqrt{x^6+5} + x^3} \\
 &= \lim_{x \rightarrow \infty} \frac{x^6+5 - x^6}{\sqrt{x^6+5} + x^3} \\
 &= \lim_{x \rightarrow \infty} \frac{5}{\sqrt{x^6+5} + x^3} = 0
 \end{aligned}$$

$$\lim_{x \rightarrow \infty} \frac{3x+5}{6x-8} = \frac{1}{2}$$

$$\frac{3x}{6x} = \frac{1}{2}$$

$$\lim_{x \rightarrow \infty} \frac{3x+5}{6x-8}$$

"Like
 $\frac{\infty}{\infty}$ " ish
sim. to $\frac{0}{0}$
YDKA

$$= \lim_{x \rightarrow \infty} \frac{x(3 + \frac{5}{x})}{x(6 - \frac{8}{x})}$$

$$= \lim_{x \rightarrow \infty} \frac{3 + \frac{5}{x}}{6 - \frac{8}{x}} = \frac{3+0}{6-0} = \frac{1}{2}$$

"to cancel out
infinities"

$$\lim_{x \rightarrow -\infty} \frac{4x^2 - x}{2x^3 - 5} \quad \frac{4x^2}{2x^3} \Rightarrow \left(\frac{2}{x} \right)$$

$$\lim_{x \rightarrow -\infty} \frac{x(4x-1)}{x(2x^2 - \frac{5}{x})} = \lim_{x \rightarrow -\infty} \frac{4x-1}{2x^2 - \frac{5}{x}}$$

$$= \lim_{x \rightarrow -\infty} \frac{x(4 - \frac{1}{x})}{x(2x - \frac{5}{x^2})} = \lim_{x \rightarrow -\infty} \frac{4 - \frac{1}{x} \nearrow 4}{2x - \frac{5}{x^2} \searrow -\infty}$$

$$\lim_{x \rightarrow -\infty} \frac{4x^2 - x}{2x^3 - 5} = \lim_{x \rightarrow -\infty} \frac{x^3 \left(\frac{4}{x} - \frac{1}{x^2} \right)}{x^3 \left(2 - \frac{5}{x^3} \right)} = 0$$

$$= \lim_{x \rightarrow -\infty} \frac{\frac{4}{x} - \frac{1}{x^2}}{2 - \frac{5}{x^3}} = \frac{0-0}{2-0} = \frac{0}{2} = 0$$

$$\lim_{x \rightarrow -\infty} \frac{x^2(4 - \frac{1}{x})}{x^3(2 - \frac{5}{x^3})}$$

$$= \lim_{x \rightarrow -\infty} \frac{4 - \frac{1}{x}}{x(2 - \frac{5}{x^3})}$$

$$= \lim_{x \rightarrow -\infty} \left(\frac{1}{x} \right) \left(\frac{4 - \frac{1}{x}}{2 - \frac{5}{x^3}} \right)$$

$$0 \left(\frac{4-0}{2} \right)$$

$$\begin{aligned}
 \lim_{x \rightarrow \infty} \sqrt{\frac{3x+5}{6x-8}} &= \sqrt{\lim_{x \rightarrow \infty} \frac{3x+5}{6x-8}} \\
 &= \sqrt{\frac{1}{2}} = \frac{\sqrt{2}}{2} \\
 &= \frac{\sqrt{1}}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{2}}{2}
 \end{aligned}$$

$$\lim_{x \rightarrow +\infty} \frac{\sqrt{x^2+2}}{3x-6}$$

$$\sqrt{a+b} \neq \sqrt{a} + \sqrt{b}$$

$$\sqrt{1+1} \stackrel{?}{=} 1+1=2$$

⋮

⌋

because $x \rightarrow +\infty$

$$\lim_{x \rightarrow +\infty} \frac{\sqrt{x^2} \cdot \sqrt{1+\frac{2}{x^2}}}{x(3-\frac{6}{x})} = \lim_{x \rightarrow +\infty} \frac{x \cdot \sqrt{1+\frac{2}{x^2}}}{x(3-\frac{6}{x})}$$

$$= \lim_{x \rightarrow +\infty} \frac{\sqrt{1+\frac{2}{x^2}}}{3-\frac{6}{x}} = \frac{\sqrt{1}}{3}$$

$$\lim_{x \rightarrow \infty} \frac{\sqrt{x^2+2}}{3x-6}$$

$$\lim_{x \rightarrow -\infty} \frac{\sqrt{x^2} \sqrt{1+\frac{2}{x^2}}}{x(3-\frac{6}{x})}$$

LKF

$$|x| = \begin{cases} x, & x \geq 0 \\ -x, & x < 0 \end{cases}$$

$$= \lim_{x \rightarrow -\infty} \frac{|x| \sqrt{1+\frac{2}{x^2}}}{x(3-\frac{6}{x})} = \lim_{x \rightarrow -\infty} \frac{(-x) \sqrt{1+\frac{2}{x^2}}}{x(3-\frac{6}{x})}$$

$$= \lim_{x \rightarrow -\infty} \frac{-\sqrt{1+\frac{2}{x^2}}}{3-\frac{6}{x}} = -\frac{1}{3}$$

$$\begin{aligned}
 & \lim_{x \rightarrow \infty} \sqrt{x^6 + 5} - x^3 \\
 & \lim_{x \rightarrow \infty} \frac{(\sqrt{x^6 + 5} - x^3)(\sqrt{x^6 + 5} + x^3)}{\sqrt{x^6 + 5} + x^3} \\
 & = \lim_{x \rightarrow \infty} \frac{(x^6 + 5) - x^6}{\sqrt{x^6 + 5} + x^3} = \lim_{x \rightarrow \infty} \frac{5}{\sqrt{x^6 + 5} + x^3} = 0
 \end{aligned}$$

